Machine Learning for Healthcare 6.871, HST.956

Lecture 21: Disease progression modeling & subtyping, Part 2

David Sontag







HEALTH SCIENCES & TECHNOLOGY

Course announcements

- Project touchpoints due Wed 4/29
- Good time to re-engage clinical mentors
 - Schedule meeting with them late this week / early next week
 - E-mail them writeup for touchpoint (CC: TA)
- Class this Thu 4/30 will be student-moderated project discussions

Recap of past two lectures

- How do we define disease?
- Genomics as a driver of major changes in precision medicine
- Clustering with clinical data to discover disease subtypes
- Prediction of disease progression from a single time-point

Outline of today's lecture

- Deep dive into data commonly used for disease progression modeling
- What can we draw inspiration from, and why they are not good enough
- Probabilistic models of disease progression
- Simultaneous staging & subtyping

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UK Biobank (from Lecture 19)

- UK Biobank collects data on ~.5M de-identified individuals
 - everyone will have full exome sequencing (50K so far)
 - 100K have worn 24-hour activity monitor for a week, 20K have had repeat measurements
 - on-line questionnaires: diet, cognitive function, work history, digestive health
 - 100K will have imaging: brain, heart, abdomen, bones, carotid artery
 - linking to EHR: death, cancer, hospital episodes, GP, blood biochemistry

We have similar biobanks in the United States, including Partners Healthcare's biobank (>40K patients), Million Veteran's Program, NIH's All of Us



Time (years)

[Poewe et al., Parkinson's disease. Nature Reviews Disease Primers, 2017]



Control Subjects without PD who are 30 years or older and who do not have a first degree blo

Actual Enrollment: 423

Enrollment Goal: 200				Actual Enrollment: 196						
Months	Sc	BL	3	6	9	12	18	24	30	36
Participants	235	198	190	184	181	185	178	174	165	167

ppmi-info.org



Figure 2-2: Correlation heatmap of MDS-UPDRS questions with subtotal annotations on the right.

Questionnaires





Figure 2-3: MDS-UPDRS subtotals for 5 PD patients



Multi-modal data

Here, e.g., including imaging

Figure 2-10: Examples of **imaging modalities**. Left to right: Top row: DaTscan, MRI axial fluid-attenuated inversion recovery, MRI axial turbo spin echo, MRI saggital magnetization-prepared rapid gradient echo. Bottom row: DTI 4-d motion trajectory, DTI eigenvectors of MRI, DTI fractional anistrophy of MRI, DTI fractional anistrophy of EPI.

Multiple myeloma: MMRF CoMMpass



myeloma/mmrf-commpass-study/

Multiple myeloma: MMRF CoMMpass

		Time
Baseline data includes RNA-seq, copy number variations, and gene mutations	Baseline Statistics	Treatments Line 3+ Line 2 Line 1
		Lab results Serum IgG

At each time step (~3 month intervals), observe blood test results:

• Immunoglobulins and antibodies (IgG, IgA, IgM, kappa chains, light chains)

• M-protein, creatinine, neutrophil count, hemoglobin, platelet count, etc.

Several of these are less frequently measured, so many missing values

Summary of challenges

- Censored data patients come in at various stages of disease progression, and leave studies early
- Irregular time intervals between observations, lots of missing data (potentially biased by healthcare processes)
- Multi-modal data (labs, symptoms, imaging, genomics)
- Limited supervision

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Learning "pseudo-time" for single-cell sequencing



[Bendall et al., Cell 2014 (human B cell development)]

Learning "pseudo-time" for single-cell sequencing



[Magwene et al., Bioinformatics, 2003; Trapnell et al., Nature Biotechnology, 2014]



RNN language models

• Could use a recurrent neural network as an autoregressive model of the distribution of observations:

$$\Pr(x_1, x_2, \dots, x_T) = \Pr(x_1) \prod_{t=2}^T \Pr(x_t \mid x_1, \dots, x_{t-1})$$

Labs, symptoms, etc.
observed at time 2

 Observations up to time t-1 summarized by RNN's hidden state h_t:

$$p_{5} = p(X_{5} \mid X_{1}, \dots, X_{4}) = p(X_{5} \mid h_{5})$$

$$(null) \rightarrow h_{1} \rightarrow h_{2} \rightarrow h_{3} \rightarrow h_{4} \rightarrow h_{5} \rightarrow h_{5} \rightarrow h_{4} \rightarrow h_{5} \rightarrow h_{$$

Why these are insufficient for disease progression modeling

- Limitations of (most) pseudo-time methods
 - Good that these handle censored data, but we often have multiple observations
 - Needs *lots* of data, but most disease data sets are small (e.g. hundreds of patients)
 - Needs simple manifolds embedded in high-dimensions; disease data sets features often low dimensional
- Limitations of (naively) using recurrent neural networks to model the sequence of observations
 - Irregular time intervals between observations^{*}
 - Missing data
 - Must model treatment effects
 - Multi-modal data

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Key idea: model patient state as a latent variable

• Use a Markov model to describe the joint distribution of patient states over time:



- State space of S could be discrete (e.g. take K states) or continuous (e.g. in R^d) – analogous to hidden state of the RNN
- If *regular* time intervals, we model the transition distribution $Pr(S_t | S_{t-1})$
- Otherwise, model $P(S_t \mid S_{t-1}, \tau_t \tau_{t-1} = \Delta)$
- Alternatively, use a Gaussian process or neural ODE to model the joint distribution of S^{*}

Deep Markov models (DMMs) of disease



- Provides an in-silico model for assessing effect of interventions (actions), by forward sampling in model
- Transition & emission distributions given by deep neural networks:



$$\mathbf{z}_t \sim \mathcal{N}(g(\mathbf{z}_{t-1}, \mathbf{u}_{t-1}), s(\mathbf{z}_{t-1}, \mathbf{u}_{t-1}))$$

[Krishnan, Shalit, Sontag, AAAI '17]

Progression modeling for diabetes

- 8000 diabetic and pre-diabetic patients
- 4 years of data, grouped into 3 month intervals
- **Observations:** 52 binary variables measuring
 - Demographics
 - Laboratory test results (e.g glucose level)
 - Diagnosis codes for conditions such as heart failure and obesity
- 200 latent dimensions for z_t

The non-linearity given by the deep neural networks significantly improves ability to model the data



Learning the effect of diabetic treatments

- Long-term: which diabetes medications work best for whom?
- Actions: 9 diabetic drugs including Metformin and Insulin (m), lab test orders (u)



• Here we just do a sanity check

Effect of diabetes treatments on glucose

w/ medication

- Align patients by when 1. they were first prescribed **Metformin**
- 2. Sample future patient data using the medications they truly received
- 3. Sample future patient data as if they never received medication



Effect of diabetes treatments on glucose



- Align patients by when they were first prescribed Metformin
- Sample future patient data using the medications they truly received
- Sample future patient data as if they never received medication



Inductive Biases for Treatment effect

 $p(z_t|z_{t-1}, u_{t-1}; \theta)$



$$\begin{split} &\lim_t = Z_t \odot \tanh(W_n \cdot [U_t; B] + b_n) \\ &\log \mathsf{cell}_t = \mathsf{LC}(Z_t, U_t, t - t_s) \\ &\mathsf{te}_t = E(t - t_s; \alpha_{1t}, \alpha_{2t}, \alpha_{3t}, \gamma_t, b_0, b_l) \\ &o_t = \sigma(\boldsymbol{\delta})_1 \odot \lim_t + \sigma(\boldsymbol{\delta})_2 \odot \mathsf{logcell}_t \\ &+ \sigma(\boldsymbol{\delta})_3 \odot \mathsf{te}_t \\ &\mu_\theta(Z_t, U_t, B) = (W_r \cdot Z_t + b_r) + o_t \end{split}$$



[Recent work by Rahul Krishnan and Zeshan Hussain]

Inductive Biases for Treatment effect

PK/PD DMM better at forecasting patient biomarkers



Held-out likelihood:	RNN	SSM Linear	SSM PK-PD	
	89.89 +/- 6.09	71.46 +/- 4.31	63.04 +/- 5.00	

[Recent work by Rahul Krishnan and Zeshan Hussain]

Alternative approach: continuous-time Markov model



- A continuous-time Markov process with irregular discrete-time observations
- The transition probability is defined by an intensity matrix and the time interval:

$$A_{ij}(\Delta) \triangleq P(S_t = j | S_{t-1} = i, \tau_t - \tau_{t-1} = \Delta; Q)$$

= expm(\Delta Q)_{ij},

Matrix Q: Parameters to learn

[Wang, Sontag, Wang, "Unsupervised learning of Disease Progression Models", KDD 2014]

Generative model for patient data



[Wang, Sontag, Wang, "Unsupervised learning of Disease Progression Models", KDD 2014]

Model of comorbidities across time



- Presence of comorbidities depends on value at previous time step and on disease stage
- Later stages of disease = more likely to develop comorbidities
- Make the assumption that once patient has a comorbidity, likely to always have it

COPD diagnosis & progression

- COPD diagnosis made using a breath test fraction of air expelled in first second of exhalation < 70%
- Most doctors use GOLD criteria to stage the disease and measure its progression:

	1 (mild)	2 (moderate)	3 (severe)	4 (very severe)		
FEV ₁ :FVC	<0.70	<0.70	<0.70	<0.70		
FEV ₁	≥80% of predicted	50–80% of predicted	30–50% of predicted	<30% of predicted or <50% of predicted plus chronic respiratory failure		
Treatment	Influenza vaccination and short-acting bronchodilator* when needed	Influenza vaccination, short-acting and ≥1 long-acting bronchodilator* when needed; consider respiratory rehabilitation	Influenza vaccination and short-acting and ≥1 long-acting bronchodilator* when needed, inhaled glucocorticosteroid if repeated exacerbations; consider respiratory rehabilitation	Influenza vaccination and short-acting and ≥1 long-acting bronchodilator* when needed, inhaled glucocorticosteroid if repeated exacerbations, long-term oxygen if chronic respiratory failure occurs; consider respiratory rehabilitation and surgery		
GOLD=Global Initiative on Obstructive Lung Disease. *β2 agonists or anticholinergics.						

Table: Therapy at each stage of chronic obstructive pulmonary disease, by GOLD stage¹

Chronic obstructive pulmonary disease. The Lancet, Volume 379, Issue 9823, Pages 1341 - 1351, 7 April 2012

Experimental evaluation

- We create a COPD cohort of 3,705 patients:
 - At least one COPD-related diagnosis code
 - At least one COPD-related drug
- Removed patients with too few records
- Clinical findings derived from 264 diagnosis codes
 - Removed ICD-9 codes that only occurred to a small number of patients
- Combined visits into 3-month time windows
- 34,976 visits, 189,815 positive findings

Inferred progression of a single patient



Prevalence of comorbidities across stages (Diabetes & Musculoskeletal disorders)



Prevalence of comorbidities across stages (Cardiovascular disease)





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Temporal heterogeneity

Patients show various disease stages through which patterns of pathology evolve



Alzheimer's disease

Frontotemporal dementia



Braak and Braak 1991

Brettschneider et al. 2014

Phenotypic heterogeneity

Individuals have different disease subtypes with distinct patterns of pathology



Alzheimer's disease

Murray et al. 2011, Whitwell et al. 2012

Frontotemporal dementia



Whitwell et al. 2012

Subtype and Stage Inference (SuStaIn)



[Young et al., Nature Communications 2018]

Conclusion

- Many open questions
 - What data is sufficient? When is it theoretically possible to disentangle subtype and stage?
 - What are sample efficient learning algorithms, good architectures for multi-modal data, …?
- Next few years, there will be an explosion of patient data from genomics, proteomics, and metabolomics
 - Will help differentiate subtypes where otherwise impossible or very difficult
 - Small sample sizes. Infrequent measurements. Modified by treatment. Confounded by comorbidities. Outcomes must still be derived from clinical data.
 - Incredible opportunity

Returning to "The Vision" from Lecture 19...

The Vision (Isaac Kohane)

A 13 year old boy presented with a recurrence of abdominal pain, hourly diarrnea and blood per rectum.

10 years earlier, he had been diagnosed with ulcerative colitis. At 3 years of age he was treated with a mild anti-inflammatory drug and had been doing very well until this most recent presentation.

On this occasion, despite the use of the full armamentarium of therapies: antimetabolites, antibiotics, glucocorticoids, immunosuppressants, first and second generation monoclonal antibody-based therapies, he continued to have pain and bloody diarrhea and was scheduled to have his colon removed. This is often but not always curative but has its own risks and consequences. After the fact, he and his parents had their exomes sequenced, which revealed rare mutations affecting specific cytokines (inflammation mediators/signalling mechanisms).

If we had plotted his position in PMMS by his proximity in clinical presentation at age 3, he would have been well within the cloud of points (each patient is a point in the above diagram) like the yellow point. If we had included the mutational profile of his cytokines he would have been identified as an outlier, like the green point. Also, if we had included his later course, where he was refractory to all therapies, he would have also been an outlier. But only if we had included the **short** duration (< 6 months) over which he was refractory to multiple medical treatments but of many years.

How do we achieve this for rare presentations and when we must learn from disparate, sparse, and messy data?