

# Machine Learning for Healthcare

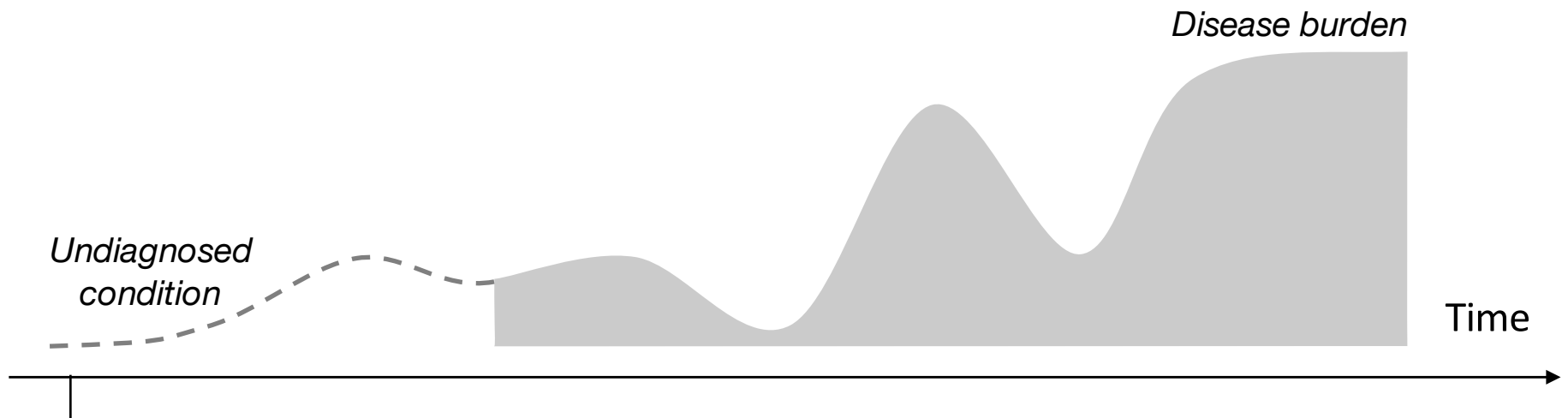
HST.956, 6.S897

## Lecture 18: Disease progression modeling & subtyping, Part 1

David Sontag



**Prognosis:** Where is a patient in their disease trajectory?  
When will the disease progress? How will treatment affect  
disease progression?



Predicted risk of developing disease or predicting outcome



**Example:** Multiple myeloma

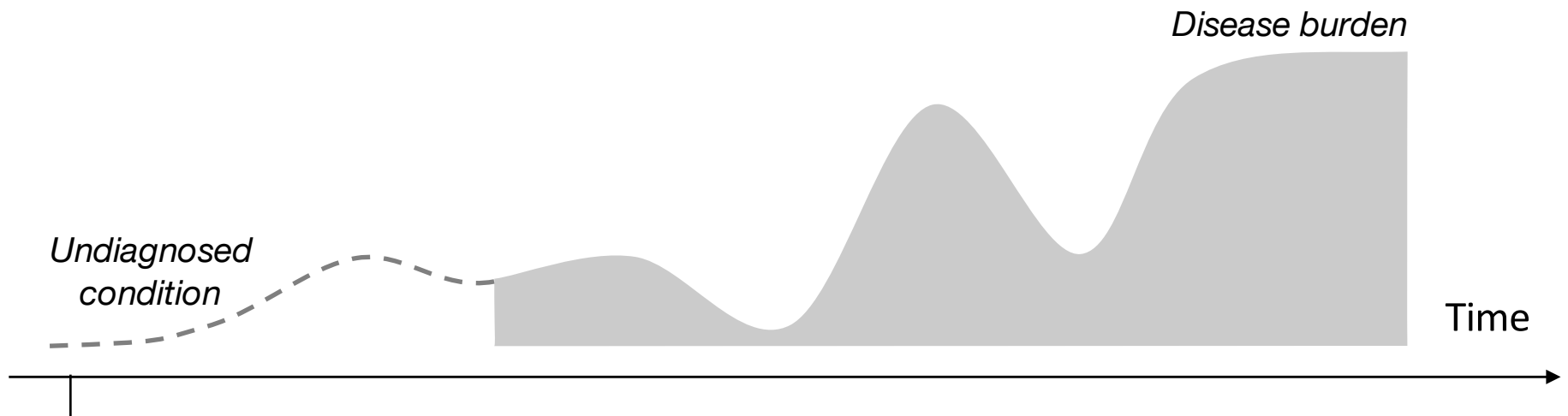
- ▶ Rare blood cancer
- ▶ MMRF CoMMpass Study has ~1000 patients

## Myeloma Staging Systems

Stage	Durie-Salmon Staging System	Revised International Staging System
I	<p>All of the following:</p> <ul style="list-style-type: none"> <li>○ Hemoglobin &gt;10.5 g/dL</li> <li>○ Serum calcium value normal or ≤12 mg/dL</li> <li>○ X-ray studies of bone, normal bone structure (scale 0) or solitary bone plasmacytoma only</li> <li>○ Low M-component production rate IgG value &lt;5 g/dL; IgA value &lt;3 g/dL</li> <li>○ Urine light chains &lt;4g/24 hours</li> </ul>	<ul style="list-style-type: none"> <li>○ Serum albumin &gt;3.5 g/dL</li> <li>○ Serum <math>\beta_2</math>-microglobulin &lt;3.5 mg/L</li> <li>○ No high-risk cytogenetics</li> <li>○ Normal serum lactate dehydrogenase level</li> </ul>
II	<p>Neither stage I nor stage III</p> <ul style="list-style-type: none"> <li>○ A—No renal failure (creatinine ≤2 mg/dL)</li> <li>○ B—Renal failure (creatinine &gt;2 mg/dL)</li> </ul>	<p>Neither stage I nor stage III</p>
III	<ul style="list-style-type: none"> <li>○ Hemoglobin value &lt;8.5 g/dL</li> <li>○ Serum calcium value &gt;12 mg/dL</li> <li>○ X-ray studies of bone, &gt;3 lytic bone lesions</li> <li>○ High M-component production rate IgG value &gt;7 g/dL; IgA value &gt;5 g/dL</li> <li>○ Urine light chains &gt;12 g/24 hours</li> </ul>	<ul style="list-style-type: none"> <li>○ Serum <math>\beta_2</math>-microglobulin &gt;5.5 mg/L</li> <li>○ High-risk cytogenetics t(4;14) t(14;16) del(17p)</li> <li>○ Elevated serum lactate dehydrogenase level</li> </ul>

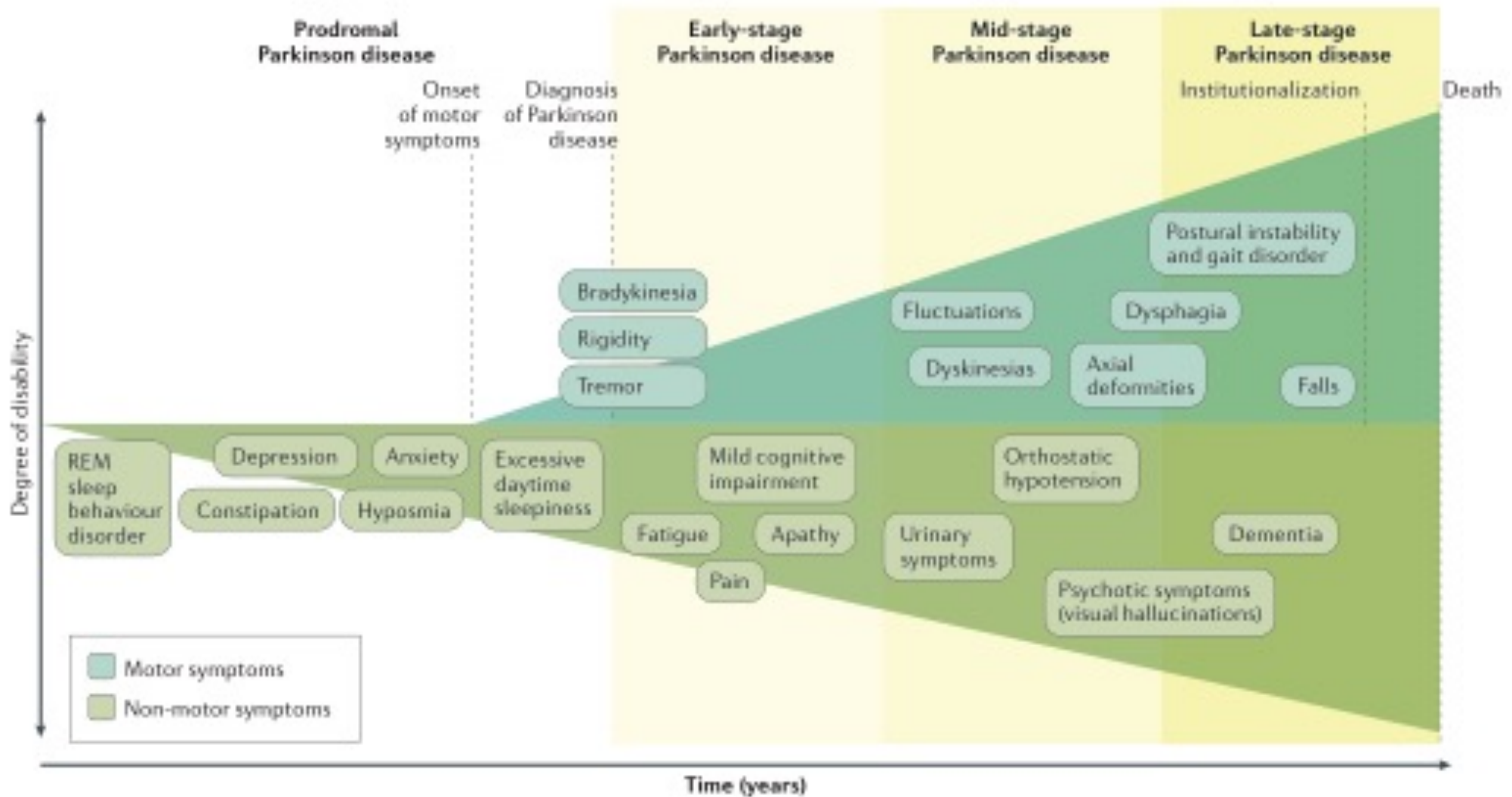
<https://www.lls.org/disease-information/myeloma/diagnosis/myeloma-staging>

## Descriptive: What does a typical trajectory look like?



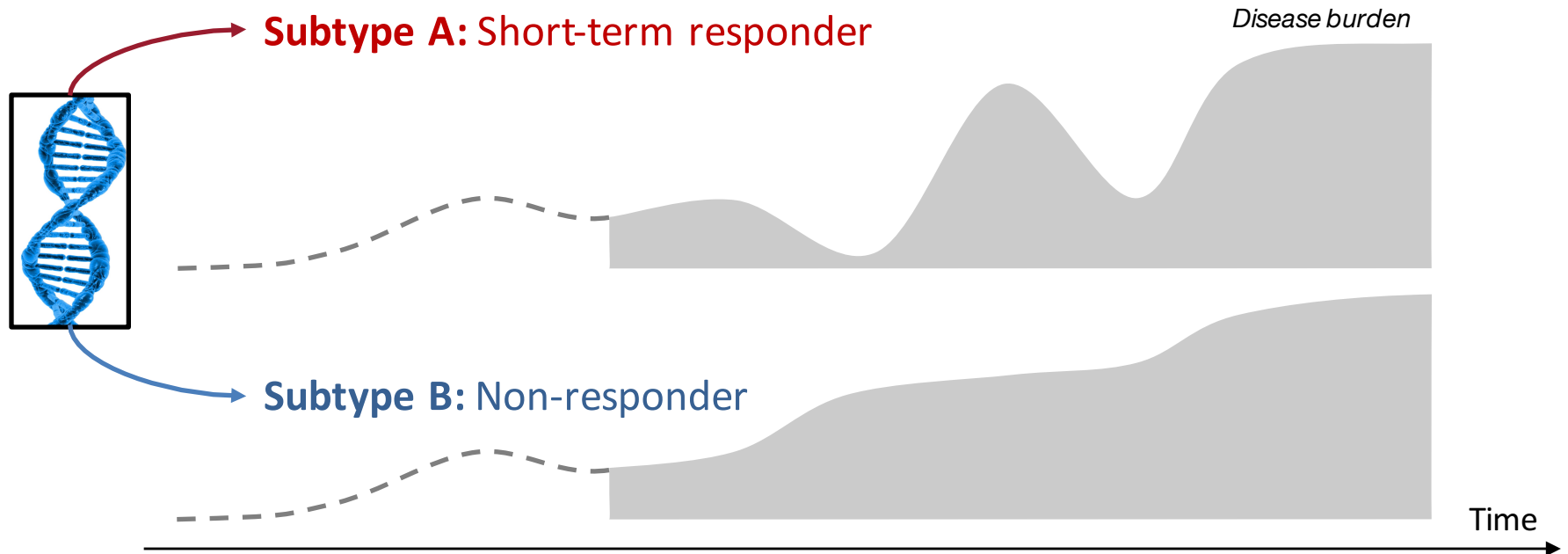
### **Example:** Parkinson's

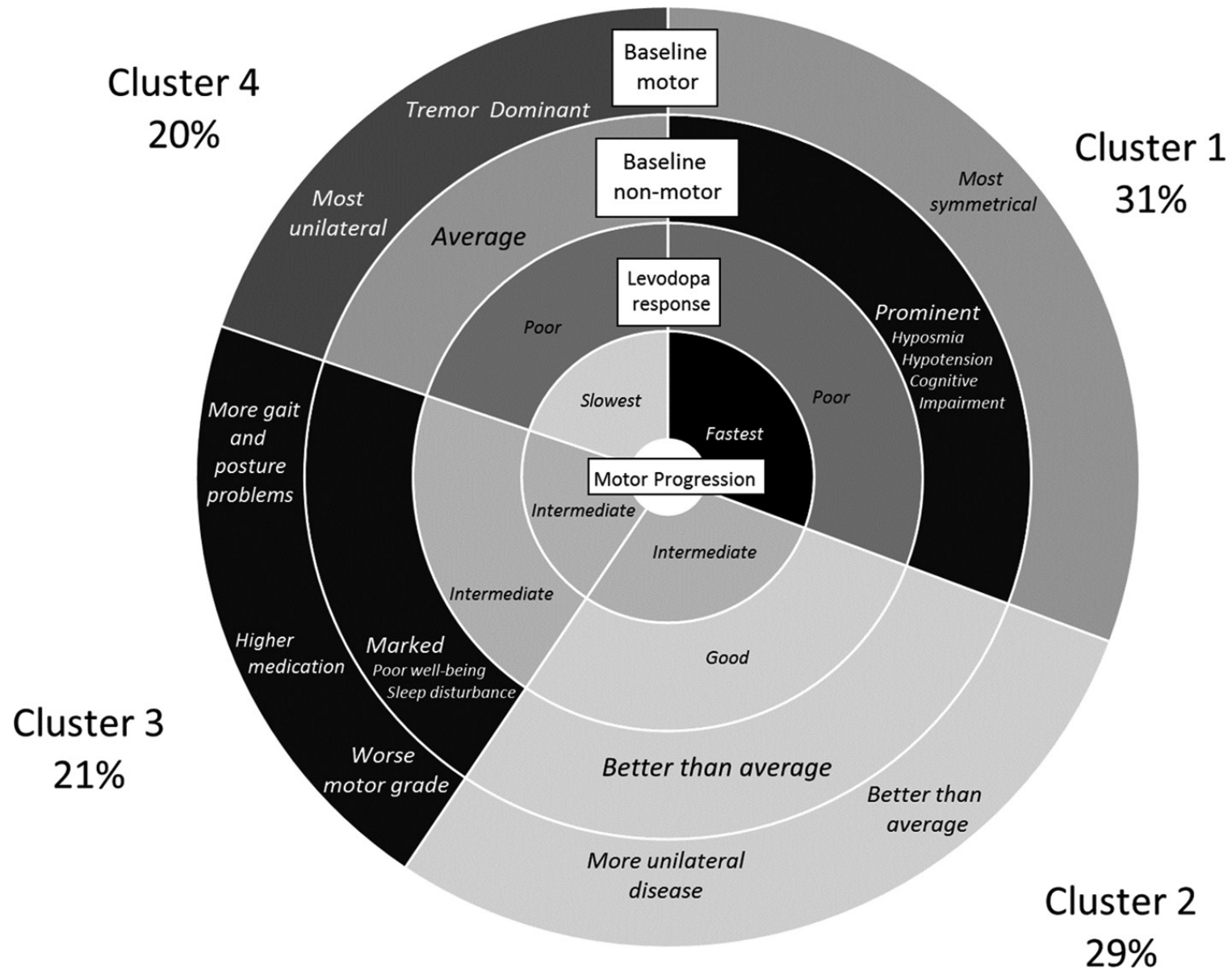
- ▶ Progressive nervous system disorder
- ▶ Affects 1 in 100 people over age 60
- ▶ PPMI dataset follows patients across time



[Poewe et al., Parkinson's disease. *Nature Reviews Disease Primers*, 2017]

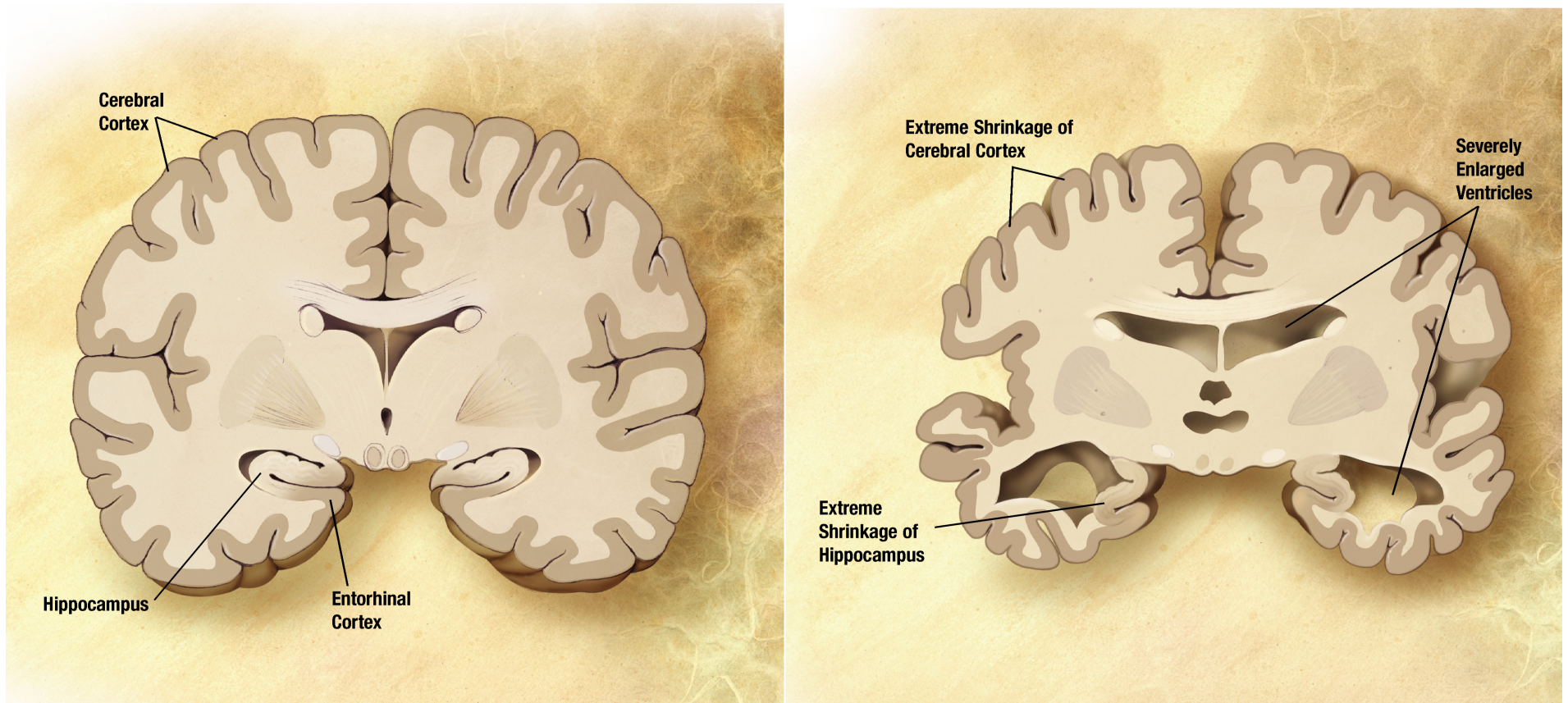
# Subtyping: Can we re-define the disease altogether?





[Lawton et al., Developing and validating Parkinson's disease subtypes and their motor and cognitive progression. *J Neurol Neurosurg Psychiatry*, 2018]

# Predicting disease progression in Alzheimer's disease



[Image credit: Wikipedia; "Alzheimer's Disease Education and Referral Center, a service of the National Institute on Aging."]



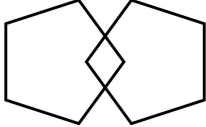
# MINI MENTAL STATE EXAMINATION (MMSE)

Name:
DOB:
Hospital Number:

Disease status  
quantified by  
cognitive score  
(continuous valued)

One point for each answer

**DATE:**

<b>ORIENTATION</b> Year    Season    Month    Date    Time  Country    Town    District    Hospital    Ward/Floor	...../ 5	...../ 5	...../ 5
<b>REGISTRATION</b> Examiner names three objects (e.g. apple, table, penny) and asks the patient to repeat (1 point for each correct. THEN the patient learns the 3 names repeating until correct).	...../ 3	...../ 3	...../ 3
<b>ATTENTION AND CALCULATION</b> Subtract 7 from 100, then repeat from result. Continue five times: 100, 93, 86, 79, 65. (Alternative: spell "WORLD" backwards: DLROW).	...../ 5	...../ 5	...../ 5
<b>RECALL</b> Ask for the names of the three objects learned earlier.	...../ 3	...../ 3	...../ 3
<b>LANGUAGE</b> Name two objects (e.g. pen, watch).  Repeat "No ifs, ands, or buts".  Give a three-stage command. Score 1 for each stage. (e.g. "Place index finger of right hand on your nose and then on your left ear").  Ask the patient to read and obey a written command on a piece of paper. The written instruction is: "Close your eyes".  Ask the patient to write a sentence. Score 1 if it is sensible and has a subject and a verb.	...../ 2	...../ 2	...../ 2
<b>COPYING:</b> Ask the patient to copy a pair of intersecting pentagons	...../ 1	...../ 1	...../ 1
			
<b>TOTAL:</b>	...../ 30	...../ 30	...../ 30

**MMSE scoring**

- 24-30: no cognitive impairment
- 18-23: mild cognitive impairment
- 0-17: severe cognitive impairment

# Predicting disease progression in Alzheimer's disease

- Goal: Predict disease status in *6, 12, 24, 36, and 48 months*
- Five different regression tasks?
- Challenge: data sparsity
  - Total number of patients is small
  - Labels are noisy
  - Due to censoring, fewer patients at later time points

# Predicting disease progression in Alzheimer's disease

- Goal: Predict disease status in 6, 12, 24, 36, and 48 months
- Five different regression tasks?
- Challenge: data sparsity

Number of patients M months after baseline  
(Alzheimer's Disease Neuroimaging Initiative)

M06	M12	M24	M36	M48
648	642	569	389	87

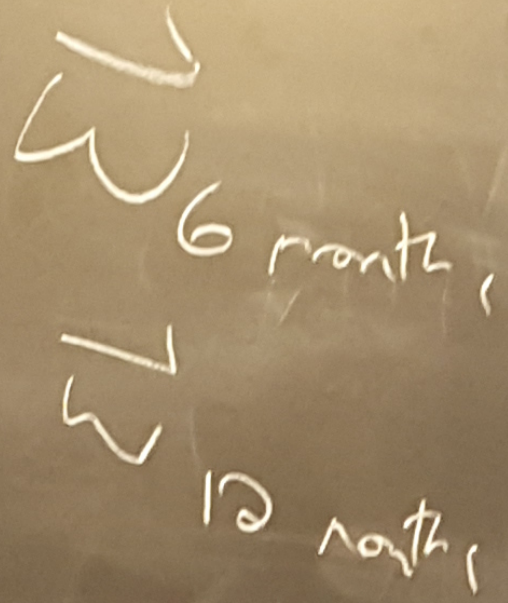
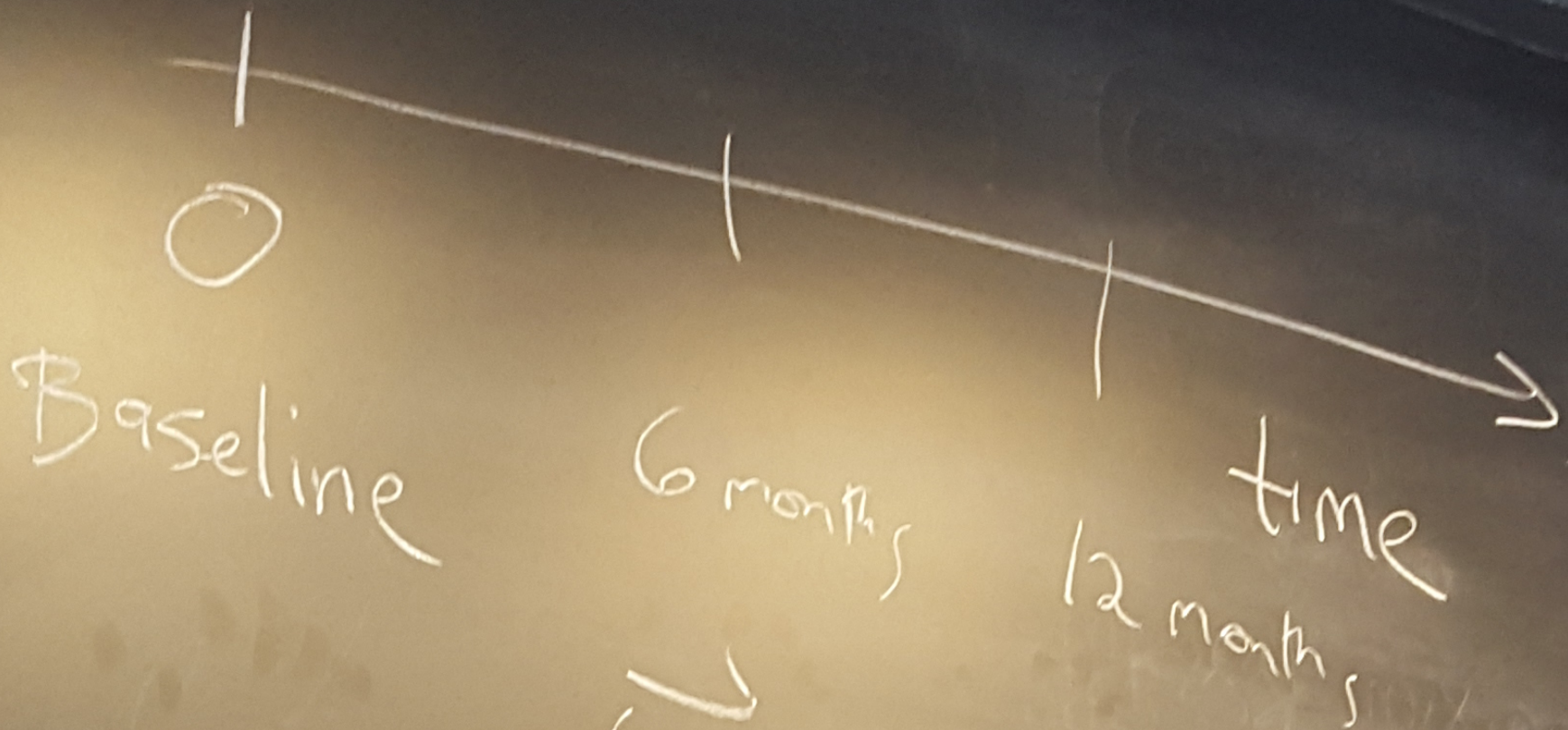
M06 = 6 months after baseline

[Zhou et al., KDD '12]

# Multi-task learning

- Goal: Predict disease status in 6, 12, 24, 36, and 48 months
- Rather than learn several independent models, view as *multi-task* learning
  - Select common set of biomarkers for all time points
  - Also allow for specific set of biomarkers at different time points
  - Incorporate temporal smoothness in models

[Zhou et al., KDD '12]



$$D_1 = \{ (\tilde{x}, y) \mid \vec{w}_1, y \in \{0, 1\} \}$$

$$D_2 = \{ (\tilde{x}, y) \mid \vec{w}_2 \}$$

$k=1, 2$

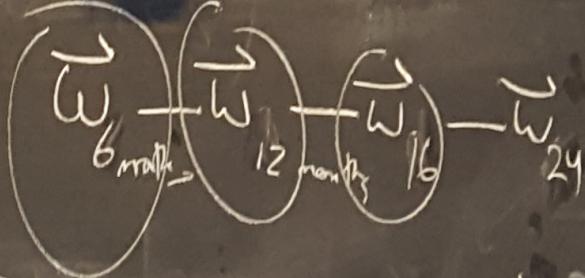
$$\min_{\vec{w}_0, \{\vec{w}_k\}_{k \in D_k}} \sum_k \max(0, 1 - y_i \tilde{x}_i \cdot \vec{w}_k) + \lambda \sum_k \|\vec{w}_k - \vec{w}_0\|_2^2$$

$\vec{w}_{16 \text{ months}}$

$\vec{w}_0$

$\vec{w}_{6 \text{ months}}$

$\vec{w}_{12 \text{ months}}$



$$\|\vec{w}_6 - \vec{w}_{12}\|_1 + \|\vec{w}_{12} - \vec{w}_{16}\|_1 + \|\vec{w}_{16} - \vec{w}_{24}\|_1$$

$$+ \frac{1}{|E|} \sum_{(i,j) \in E} \|\vec{w}_i - \vec{w}_j\|^2$$

# Convex fused sparse group lasso

- Simultaneously learn all 5 models by solving the following convex optimization problem:

$$\min_W L(W) + \lambda_1 \|W\|_1 + \lambda_2 \left\| RW^T \right\|_1 + \lambda_3 \|W\|_{2,1}$$

- Squared loss:  $L(W) = \|S \odot (XW - Y)\|_F^2$   
( $S$  is a mask to account for labels missing in subset of tasks)

- Group Lasso penalty  $\|W\|_{2,1}$  given by  $\sum_{i=1}^d \sqrt{\sum_{j=1}^t W_{ij}^2}$

- $R =$ 

				5
	1	-1		
		1	-1	
4			1	-1

[Zhou et al., KDD '12]



# Features

MRI scans (white matter parcellation volume, etc.) +

Demographic	age, years of education, gender
Genetic	ApoE- $\epsilon$ 4 information
Baseline cognitive scores	MMSE, ADAS-Cog, ADAS-MOD, ADAS subscores, CDR, FAQ, GDS, Hachinski, Neuropsychological Battery, WMS-R Logical Memory
Lab tests	RCT1, RCT11, RCT12, RCT13, RCT14, RCT1407, RCT1408, RCT183, RCT19, RCT20, RCT29, RCT3, RCT392, RCT4, RCT5, RCT6, RCT8

**371 in total**

[Zhou et al., KDD '12]

# Results (averaged over 5 time points)

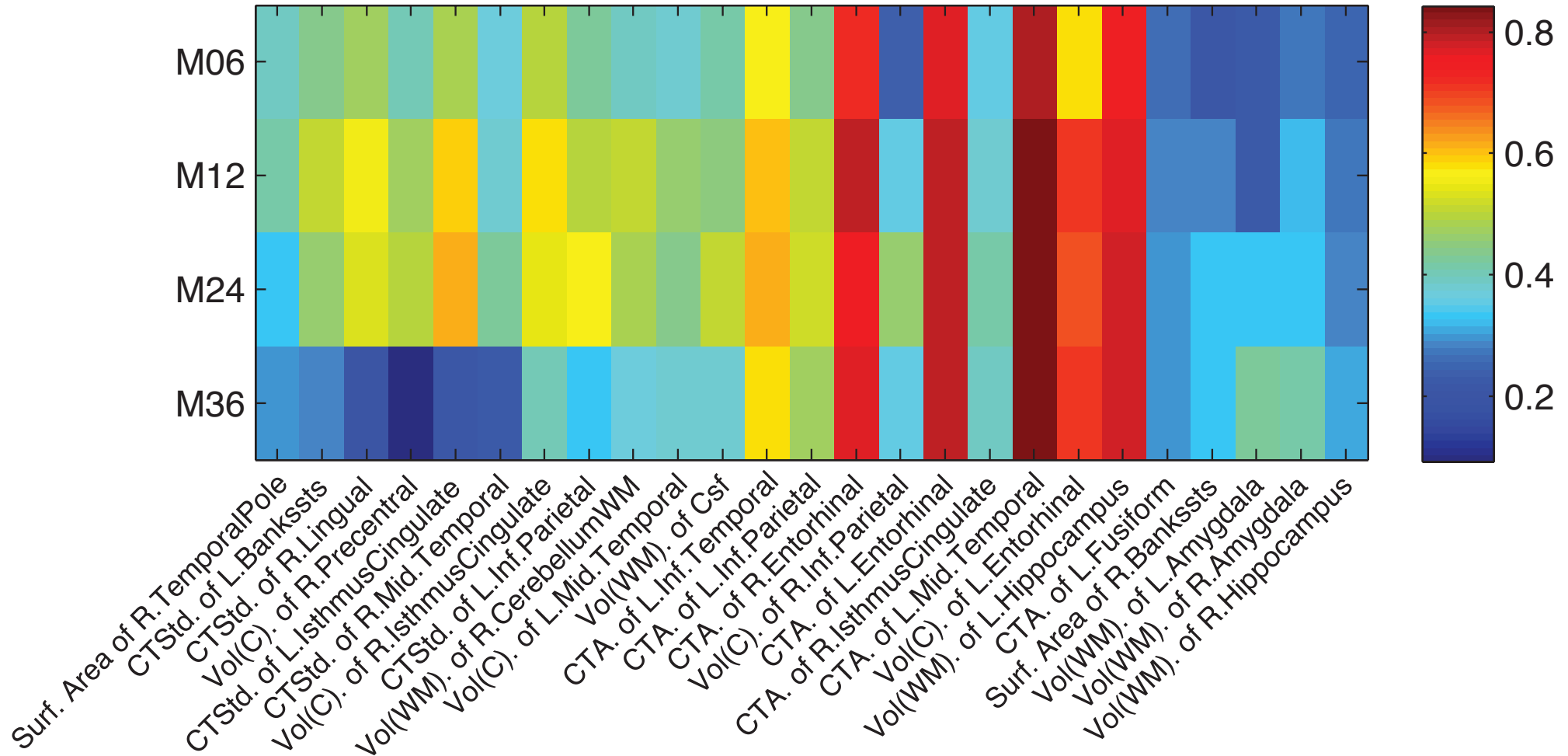
Baseline – independent regressors		Temporal smoothing helps!		
		$\lambda_2 = 20$	$\lambda_2 = 50$	$\lambda_2 = 100$
Ridge		cFSGL1	cFSGL2	cFSGL3
Target: MMSE				
nMSE	$0.548 \pm 0.057$	$0.428 \pm 0.052$	$0.400 \pm 0.053$	<b><math>0.395 \pm 0.052</math></b>
R	$0.689 \pm 0.030$	$0.772 \pm 0.030$	$0.790 \pm 0.032$	<b><math>0.796 \pm 0.031</math></b>

nMSE – normalized mean squared error. Smaller is better

R – average  $R^2$  (correlation coefficient). Larger is better

$$\min_W L(W) + \lambda_1 \|W\|_1 + \lambda_2 \left\| RW^T \right\|_1 + \lambda_3 \|W\|_{2,1}$$

# Feature importance varies by time



(a) Target: ADAS-Cog (25 stable features)

# Can we use an unsupervised approach?

- Twin goals:

- **Discover disease subtypes:**

Want to describe heterogeneity in a way that can be easy to act on (i.e., interpretable)

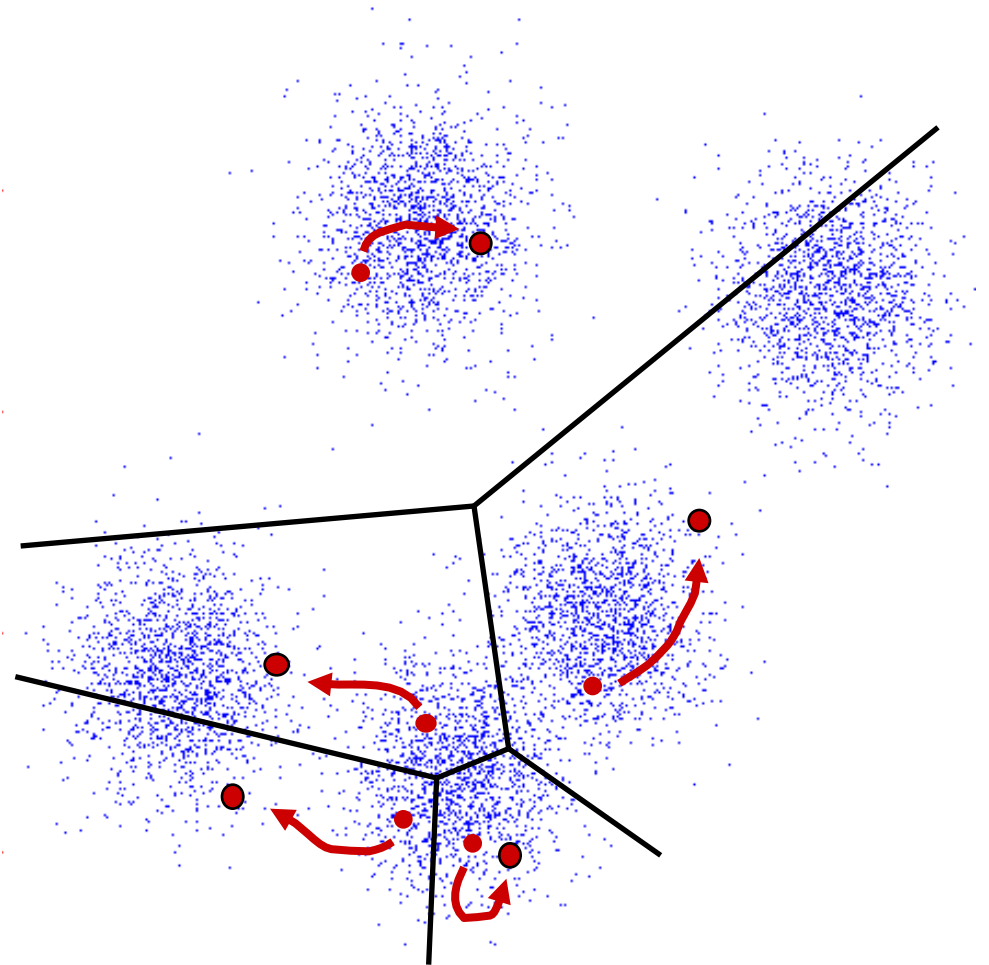
Not *just* interested in prediction – rather, identify cohorts for clinical trials, better understand disease mechanism

- **Make use of similarity of individuals at baseline**

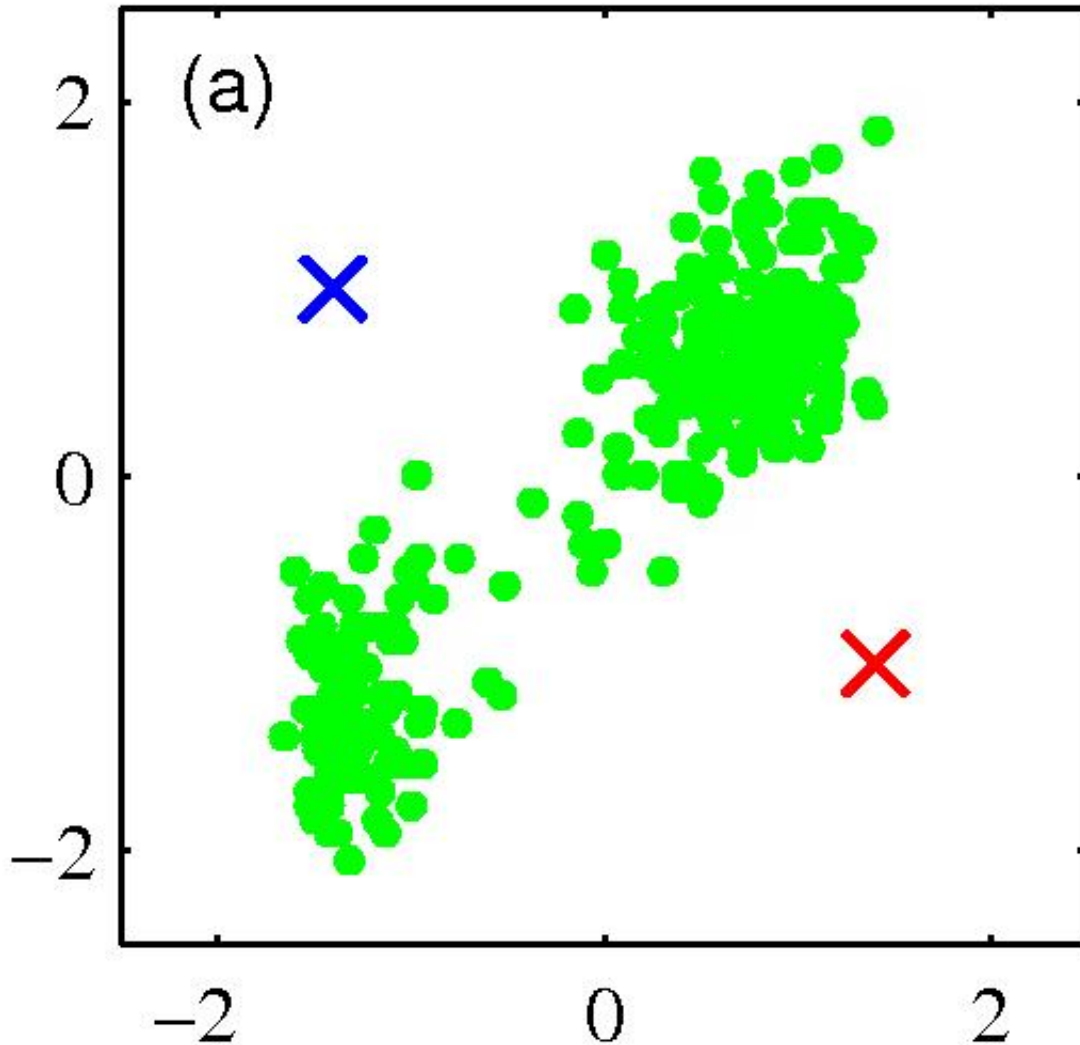
Dimensionality reduction to prevent overfitting

# K-Means

- An iterative clustering algorithm
  - **Initialize:** Pick  $K$  random points as cluster centers
  - **Alternate:**
    1. Assign data points to closest cluster center
    2. Change the cluster center to the average of its assigned points
  - **Stop** when no points' assignments change



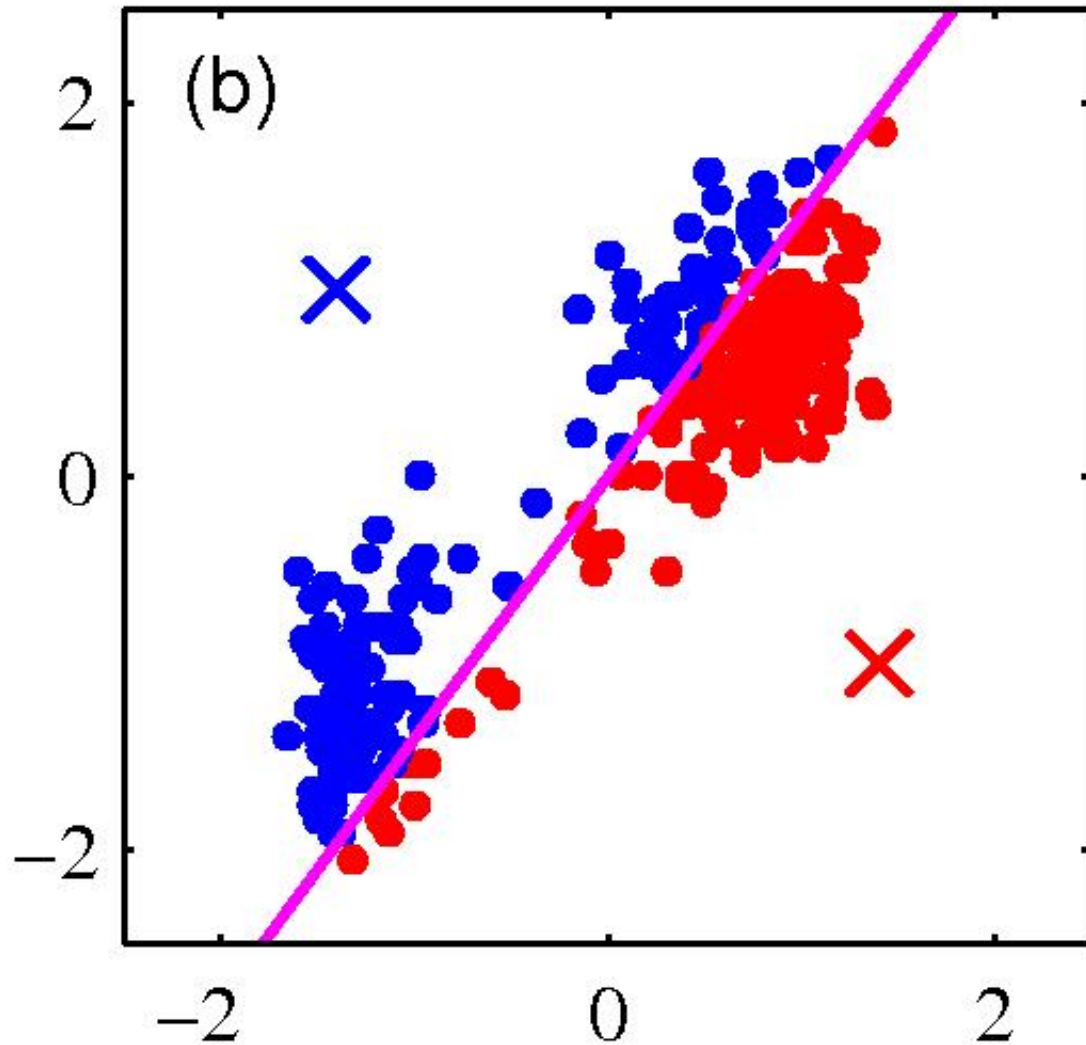
# K-means clustering: Example



- Pick  $K$  random points as cluster centers (means)

Shown here for  $K=2$

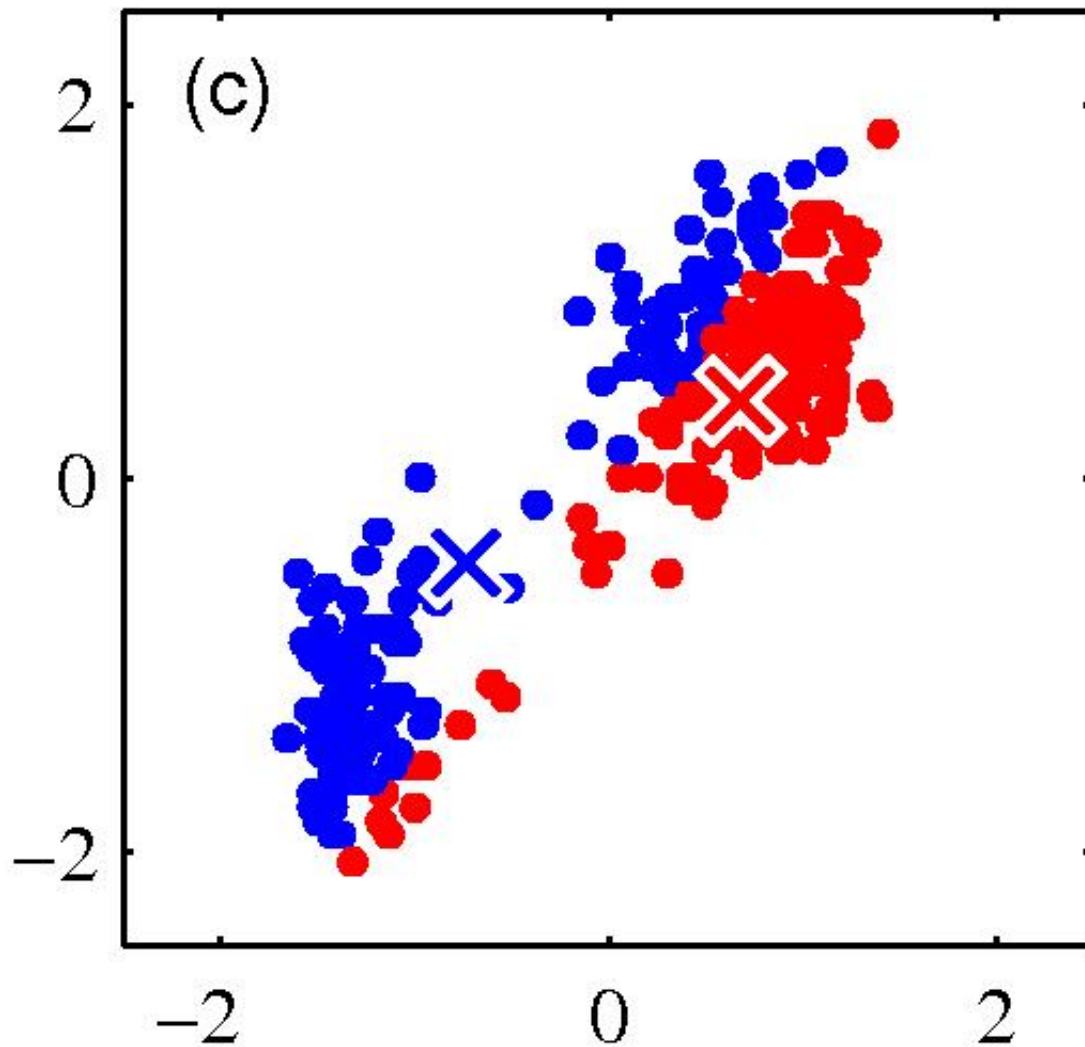
# K-means clustering: Example



Iterative Step 1

- Assign data points to closest cluster center

# K-means clustering: Example

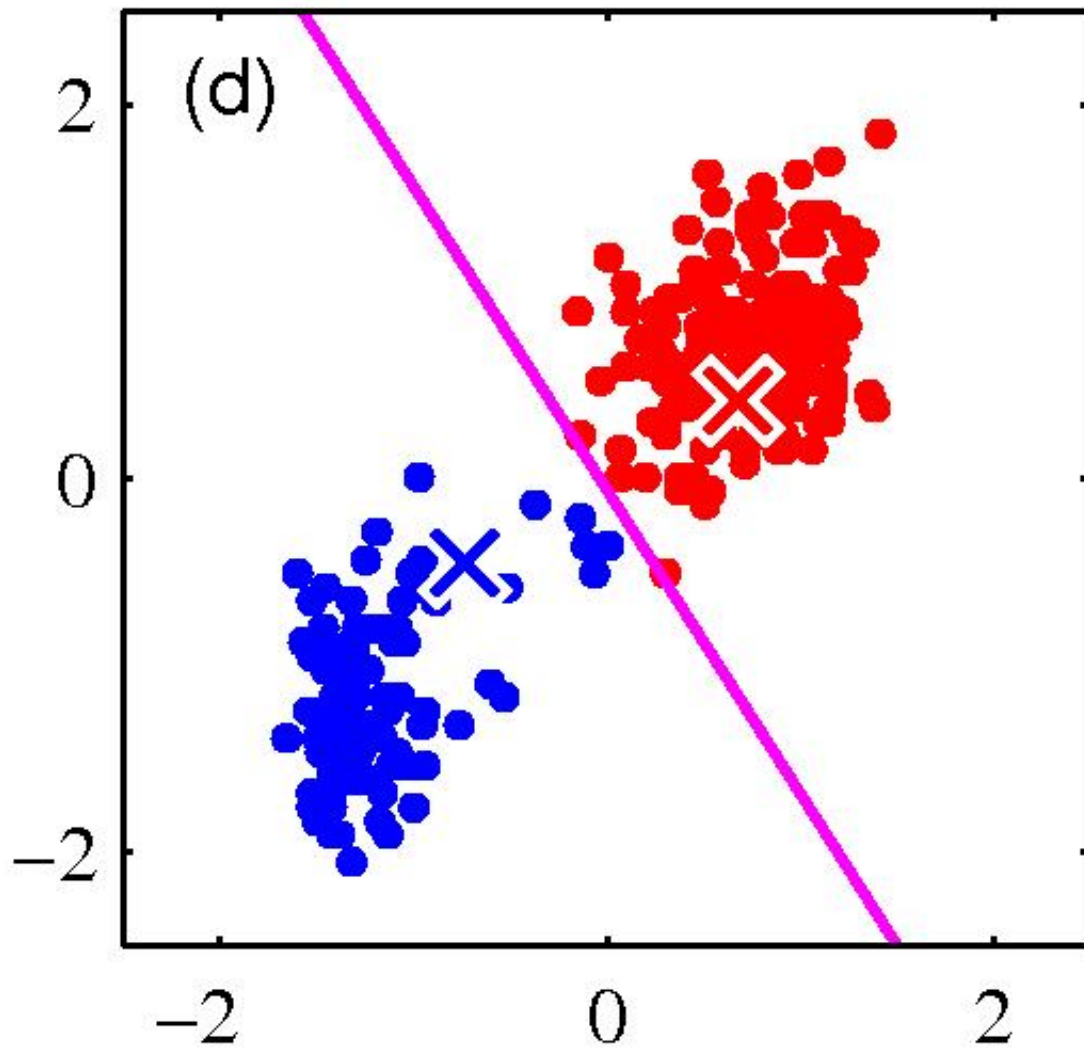


## Iterative Step 2

- Change the cluster center to the average of the assigned points



# K-means clustering: Example



- Repeat until convergence

# Asthma: the problem

- 5 to 10% of people with severe asthma remain poorly controlled despite maximal inhaled therapy

[Holgate ST, Polosa R. The mechanisms, diagnosis, and management of severe asthma in adults. *Lancet*. 2006; 368:780–793]



[[whatasthma.com](http://whatasthma.com)]

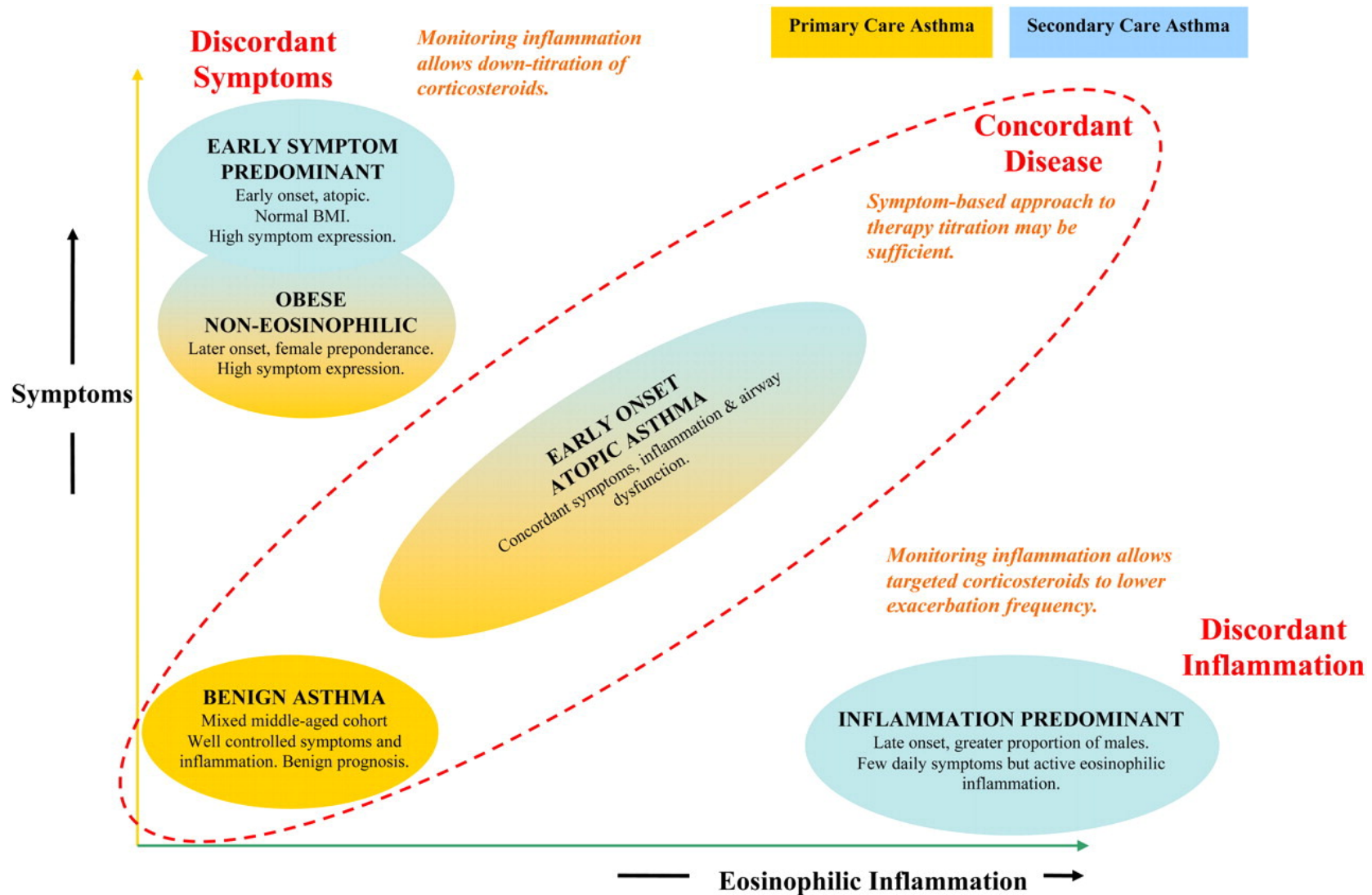
# Asthma: the question

**“It is now recognised that there are distinct asthma phenotypes and that distinct therapeutic approaches may only impinge on some aspects of the disease process within each subgroup”**

- What are the processes (genetic or environmental) that underlie different subtypes of asthma?
- Which aspects of airway remodelling are important in disease subtypes?
- What are the best biomarkers of disease progression or treatment response?
- Why are some patients less responsive to conventional therapies than others?

[Adcock et al., “New targets for drug development in asthma”. The Lancet, 2008]

# Discovering subtypes from data



[Haldar et al., *Am J Respir Crit Care Med*, 2008]

# The data

- All patients had physician diagnosis of asthma and at least one recent prescription for asthma therapy
- All were current nonsmokers
- *Data set #1*: 184 patients recruited from primary-care practices in the UK
- *Data set #2*: 187 patients from refractory asthma clinic in the UK
- *Data set #3*: 68 patients from 12 month clinical study
- Features: z scores for continuous variables, 0/1 for categorical
  - Some of the continuous variables log-transformed to approximate a normal distribution

## Comparison of Baseline Characteristics in the three Asthma Populations

Variable	Primary Care (n = 184)	Secondary Care (n = 187)	Longitudinal Cohort (n = 68)
Sex, % female	54.4	65.8	47.1
Age, yr (SD)	49.2 (13.9)	43.4 (15.9)	52.4 (14.6)
Age of onset, yr (SD)	24.7 (19)	20.3 (18.4)	31.1 (23.7)
Atopic status, % positive	72.8	73.8	57.4
Body mass index, kg/m <sup>2</sup> (SD)	27.5 (5.4)	28.5 (6.5)	28.0 (5.9)
PC <sub>20</sub> methacholine <sup>†</sup> , mg/ml	1.04 (1.13)	†	0.67 (0.68)
Peak flow variability, amp % mean	17 (0.38)	32.2 (0.48)	13.8 (0.29)
FEV <sub>1</sub> change with bronchodilator, %	1.63 (1.16)	12.8 (0.41)	3.2 (1.04)
Post-bronchodilator FEV <sub>1</sub> , % predicted	91.4 (21)	82.1 (21.1)	80.2 (20.6)
Sputum eosinophil count, %	1.32 (0.62)	2.9 (0.99)	2.4 (0.81)
FE <sub>NO</sub> <sup>‡</sup> , ppb	31.6 (0.33)	43 (0.32)	4.32 (0.64) <sup>‡</sup>
Sputum neutrophil count, %	55.09 (0.31)	46.7 (0.32)	41.1 (0.35)
Modified JACS <sup>§</sup> (SD)	1.36 (0.74)	2.02 (1.16)	1.42 (1.26)
Dose of inhaled corticosteroid, BDP equivalent/ $\mu$ g (SD)	632 (579)	1,018 (539)	1,821 (1,239)
Long-acting bronchodilator use, %	40.2	93	86.7

*Definition of abbreviations:* amp = amplitude; BDP = beclomethasone dipropionate; JACS = Juniper Asthma Control Score

[Haldar et al., *Am J Respir Crit Care Med*, 2008]

Clusters in  
primary  
care  
  
(found by  
K-means)

Variable	Primary Care (n = 184)	Cluster 1	Cluster 2	Cluster 3	Significance (P Value)*
		Early-Onset Atopic Asthma (n = 61)	Obese Noneosinophilic (n = 27)	Benign Asthma (n = 96)	
Sex <sup>†</sup> , % female	54.4	45.9	81.5	52.1	0.006
Age, yr (SD)	49.2 (13.9)	44.5 (14.3)	53.9 (14)	50.8 (13)	0.003
Age of onset <sup>†</sup> , yr (SD)	24.7 (19)	14.6 (15.4)	35.3 (19.6)	28.2 (18.3)	<0.001
Atopic status <sup>†</sup> , % positive	72.8	95.1	51.9	64.6	<0.001
Body mass index <sup>†</sup> , kg/m <sup>2</sup> (SD)	27.5 (5.4)	26.1 (3.8)	36.2 (5.5)	26 (3.6)	<0.001
PC <sub>20</sub> methacholine <sup>†‡</sup> , mg/ml	1.04 (1.13)	0.12 (0.86)	1.60 (0.93)	6.39 (0.75)	<0.001
PC <sub>20</sub> >8 mg/ml, n (%)	64 (34.7)	2 (3.3)	6 (22.2)	56 (58.3)	<0.001
Peak flow variability <sup>†‡</sup> , amp % mean	17 (0.38)	20 (0.47)	21.9 (0.32)	14.8 (0.32)	0.039
FEV <sub>1</sub> change with bronchodilator <sup>‡</sup> , %	1.63 (1.16)	4.5 (0.91)	1.82 (1.16)	0.83 (1.22)	<0.001
Post-bronchodilator FEV <sub>1</sub> , % predicted	91.4 (21)	86.9 (20.7)	91.5 (21.4)	94.2 (20.7)	0.107
Sputum eosinophil count <sup>†‡</sup> , %	1.32 (0.62)	3.75 (0.64)	1.55 (0.51)	0.65 (0.44)	<0.001
FE <sub>NO</sub> <sup>‡§</sup> , ppb	31.6 (0.33)	57.5 (0.27)	25.8 (0.29)	22.8 (0.27)	<0.001
Sputum neutrophil count <sup>‡</sup> , %	55.09 (0.31)	45.87 (0.24)	72.71 (0.13)	57.56 (0.36)	0.038
Modified JACS <sup>†</sup> (SD)	1.36 (0.74)	1.54 (0.58)	2.06 (0.73)	1.04 (0.66)	<0.001
Dose of inhaled corticosteroid, BDP equivalent/ $\mu$ g (SD)	632 (579)	548 (559)	746 (611)	653 (581)	0.202
Long-acting bronchodilator use, %	40.2	34.4	48.2	41.7	0.442
Previous hospital admission or emergency attendance, no. per patient	0.60 (1.57)	1.04	0.26	0.20	0.037
Previous outpatient attendance, % attended	15%	22%	19%	6%	0.121
Severe asthma exacerbations (requiring oral corticosteroids) in past 12 mo, no. per patient	1.25 (1.94)	1.86 (0.32)	1.07 (0.32)	0.39 (0.18)	0.002

# Clusters in secondary care

Variable	Secondary Care (n = 187)	Cluster 1	Cluster 2	Cluster 3	Cluster 4	Significance (P Value)*
		Early Onset, Atopic (n = 74)	Obese, Noneosinophilic (n = 23)	Early Symptom Predominant (n = 22)	Inflammation Predominant (n = 68)	
Sex †, % female	<b>65.8</b>	<div style="border: 1px solid black; padding: 5px; text-align: center;"> <p style="color: red; font-weight: bold;">Resembled clusters from primary care – i.e., these are common across spectrum of severity</p> <p style="font-weight: bold;">Objective measures of disease severity show more advanced disease</p> </div>		68.2	47.1	<0.001
Age, yr (SD)	<b>43.4 (15.9)</b>			35.5 (15.5)	50.6 (15.1)	<0.001
Age of onset †, yr (SD)	<b>20.3 (18.4)</b>			12.6 (15)	32.6 (19.1)	<0.001
Atopic status †, % positive	<b>73.8</b>			81.8	63.2	0.024
Body mass index †, kg/m <sup>2</sup> (SD)	<b>28.5 (6.5)</b>			23.6 (3.1)	27 (3.9)	<0.001
Peak flow variability ‡, amp % mean	<b>32.2 (0.48)</b>			24.2 (0.65)	27.6 (0.36)	0.002
FEV <sub>1</sub> change with bronchodilator ‡, %	<b>12.8 (0.41)</b>	24.5 (0.31)	9.3 (0.35)	4.5 (0.33)	9.8 (0.34)	<0.001
Post-bronchodilator FEV <sub>1</sub> , % predicted (SD)	<b>82.1 (21.1)</b>	79.0 (21.9)	79.0 (18.5)	79.5 (26.1)	87.2 (18.5)	0.093
Sputum eosinophil count †‡, %	<b>2.9 (0.99)</b>	4.2 (0.76)	1.3 (1.01)	0.1 (0.9)	8.4 (0.64)	<0.001
FE <sub>NO</sub> ‡§, ppb	<b>43 (0.32)</b>	51.2 (0.36)	24.2 (0.27)	22.6 (0.30)	53.1 (0.32)	<0.001
Sputum neutrophil count, % ‡	<b>46.7 (0.32)</b>	45.4 (0.39)	49.3 (0.22)	51.3 (0.23)	45.9 (0.29)	0.892
Modified JACS † (SD)	<b>2.02 (1.16)</b>	2.63 (0.93)	2.37 (1.09)	2.11 (1.11)	1.21 (0.95)	<0.001
Dose of inhaled corticosteroid, BDP equivalent/μg (SD)	<b>1,018 (539)</b>	1,168 (578)	1,045 (590)	809 (396)	914 (479)	0.008
Long-acting bronchodilator use, %	<b>93.0</b>	91.9	95.4	90.9	94.1	0.999



# How should we treat asthma?

- Now we use 3<sup>rd</sup> dataset – 68 patients over 12 months
- Randomized control trial with two arms:
  - Standard clinical care (“clinical”)
  - Regular monitoring of airway inflammation using induced sputum, to titrate steroid therapy to maintain normal eosinophil counts (“sputum”)
- Original study found no difference in corticosteroid usage
  - But, this could have been explained by heterogeneity in treatment response!

# Patients in different clusters respond differently to treatment! (analysis using 3<sup>rd</sup> dataset from 12 month study)

Cluster (found using <i>baseline</i> data)	Outcomes	Treatment strategy		Significance
		Clinical ( <i>n</i> = 10)	Sputum ( <i>n</i> = 8)	
1: Obese female	Δ Inhaled corticosteroid dose <sup>*</sup> /μg per day (SEM)	-400 (328)	-462 (271)	0.89
	Severe exacerbation frequency over 12 mo (SEM)	1.40 (0.78)	1.50 (0.80)	0.93
	Number commenced on oral corticosteroids	2	1	0.59
		Clinical ( <i>n</i> = 15)	Sputum ( <i>n</i> = 24)	
2: Inflammation predominant	Δ Inhaled corticosteroid dose <sup>*</sup> /μg per day (SEM)	+753 (334)	+241 (233)	0.22
	Severe exacerbation frequency over 12 mo (SEM)	3.53 (1.18)	0.38 (0.13)	0.002
	Number commenced on oral corticosteroids	2	9	0.17
		Clinical ( <i>n</i> = 7)	Sputum ( <i>n</i> = 4)	
3: Early symptom predominant	Δ Inhaled corticosteroid dose <sup>*</sup> /μg per day (SEM)	+1,429 (429)	-400 (469)	0.022
	Severe exacerbation frequency over 12 mo (SEM)	5.43 (1.90)	2.50 (0.87)	0.198
	Number commenced on oral corticosteroids	6	0	Undefined

[Haldar et al., *Am J Respir Crit Care Med*, 2008]

# Summary – two approaches

- **Supervised:**  
predict future disease status
- **Unsupervised:**  
which patients look similar / different? Do clusters have different outcomes?

# Limitations that we'll address in the next lecture

- Can't differentiate between *stage* and *subtype*
  - Patients assumed to be aligned at baseline
- Only make use of one time point per patient
- Assumes single factor (cluster) explains all variation
- Distance function is particularly simplistic
- Either supervised or unsupervised, but not both – how to combine?